



# Reference Week Adjustment for Employment Insurance Statistics

November 20, 2019

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Delivering insight through data for a better Canada

# Agenda

- Overview of Employment Statistics Program
- Reference Week
- Issues Encountered During Seasonal Adjustment (SA)
- Solution 1: Modelling
- Solution 2: Alternative Data Source

# Overview of EI Statistics Program

- EI Statistics Program:
  - Monthly estimates
  - Statistics on number of EI beneficiaries, number of claims, type of benefits, number of disqualifications and disentitlements.
  - Uses administrative data: administered by Service Canada on behalf of Employment and Social Development Canada
  - Data seasonally adjusted (X-12-ARIMA)

# Reference Week

- Reference Week (RW): The **week** containing the **15<sup>th</sup>** day of the month
- Number of beneficiaries obtained by counting number of people who qualified for EI benefits during the reference week (whether or not they have received benefits for other weeks)
- Reference week introduces a calendar effect due to location of the 15<sup>th</sup> day.
- Impacts month-to-month change in the EI statistical estimates.

MONTH						
SUN	MON	TUE	WED	THU	FRI	SAT
			1	2	3	4
5	6	7	8	9	10	11
12	13	14	15	16	17	18
19	20	21	22	23	24	25
26	27	28	29	30	31	

# Issues Encountered During Seasonal Adjustment

- Prior to 2017: beneficiaries wait 2 weeks before receiving EI benefits.
- Adjustment is made relative to where the 15<sup>th</sup> falls compared to Wednesday; done via a linear regARIMA model:

$$y_t = \sum_i \beta_i x_{it} + z_t, \quad z_t \sim \text{ARIMA}$$

- where:
  - $y_t$  is the dependent time series
  - $x_{it}$  are the regression variables depending on time  $t$
  - $\beta_i$  are the regression parameters
  - $z_t$  are the regression residuals

# Issues Encountered During Seasonal Adjustment

Positive adjustment

MONTH						
SUN	MON	TUE	WED	THU	FRI	SAT
	1	2	3	4	5	6
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30	31			

Negative adjustment

MONTH						
SUN	MON	TUE	WED	THU	FRI	SAT
						1
2	3	4	5	6	7	8
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29
30	31					

←  $x_{it} = +2$

$x_{it} = \delta_{it} - 15$   
 where  $\delta_{it}$  is Wednesday's date during RW

→  $x_{it} = -3$


# Issues Encountered During Seasonal Adjustment

- As of 2017: new legislation changed the waiting period to one week. 

**Before 2017:**  
2 week waiting period



**As of 2017:**  
1 week waiting period

- This introduced a problem for the reference week adjustment we were using. 
- Most beneficiaries would request EI benefits at end of month:
  - Before 2017: Waiting period often intersects reference week
  - After 2017: Waiting period rarely intersects reference week (big impact on Health and Education sectors)

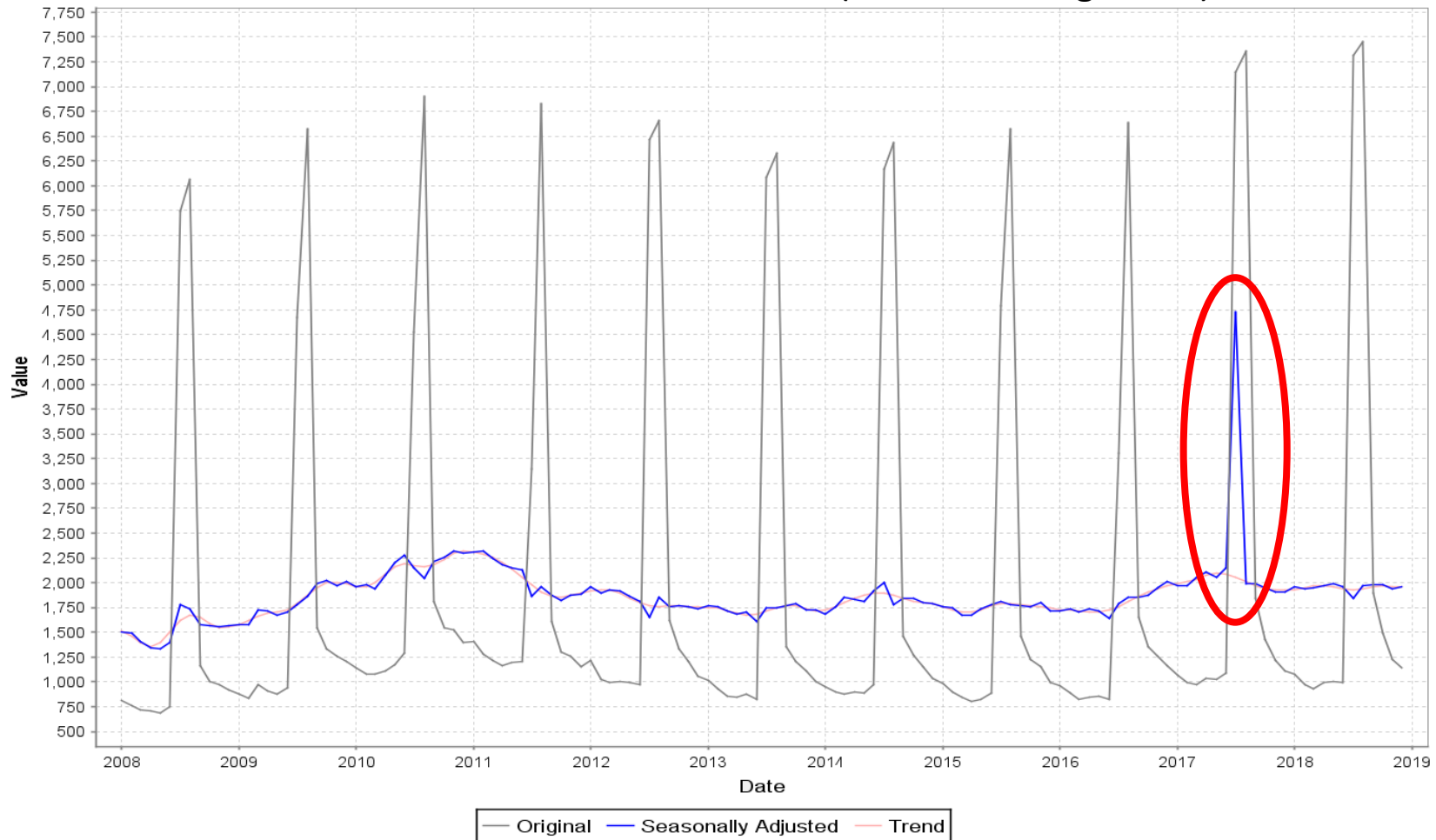
# Issues Encountered During Seasonal Adjustment

- As of 2017, reference week adjustment did not seem necessary
- Keeping the linear reference week adjustment: spikes in the data would be introduced post-2017.
- Removing the reference week adjustment: spikes introduced in pre-2017 data.
- Obviously, the linear regressor was not working as we wanted.
- Had to think of a new solution to take care of this problem.



# Issues Encountered During Seasonal Adjustment

Beneficiaries, Manitoba, Education (with linear regressor)



# Solution 1: Use Various Non-Linear Models

- Here, we tried various non-linear models and compared to linear model:

- $f(x_{it}) = \sqrt[3]{x_{it}}$
- $f(x_{it}) = \exp(x_{it})$
- $f(x_{it}) = x_{it}^2$
- $f(x_{it}) = x_{it}^2 + x_{it}$
- $f(x_{it}) = \text{expit}(x_{it})$

$$\text{expit}(x_{it}) = \text{logit}^{-1}(x_{it}) = \log^{-1}\left(\frac{x_{it}}{1 - x_{it}}\right) = \frac{\exp(x_{it})}{\exp(x_{it}) + 1}$$

- 1341 series: 6 models, 12 months → 96,552 results

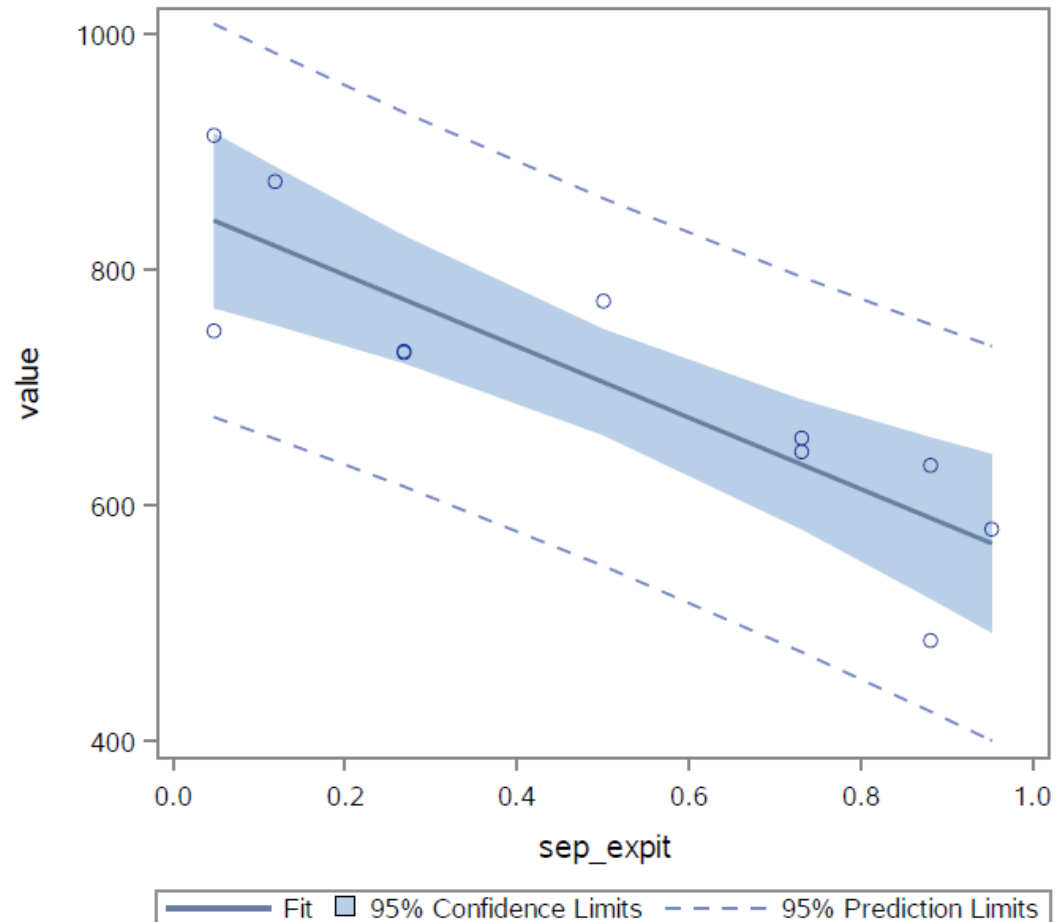
# Solution 1: Use Various Non-Linear Models

- Looking at the best model fit for each month based on  $R^2_{adj}$ , AIC, BIC (16,092 models)

$R^2_{adj}$		AIC		BIC	
Model	% Frequency	Model	% Frequency	Model	% Frequency
Linear	5.56	Linear	6.05	Linear	6.33
Cube root	21.11	Cube root	22.20	Cube root	23.01
Exponential	11.38	Exponential	12.93	Exponential	13.97
Quadratic	37.61	Quadratic	42.09	Quadratic	44.44
Quadratic with linear term	17.83	Quadratic with linear term	9.57	Quadratic with linear term	4.72
Expit	6.50	Expit	7.16	Expit	7.53

# Solution 1: Use Various Non-Linear Models

Beneficiaries, Manitoba, Education: Explit model for September

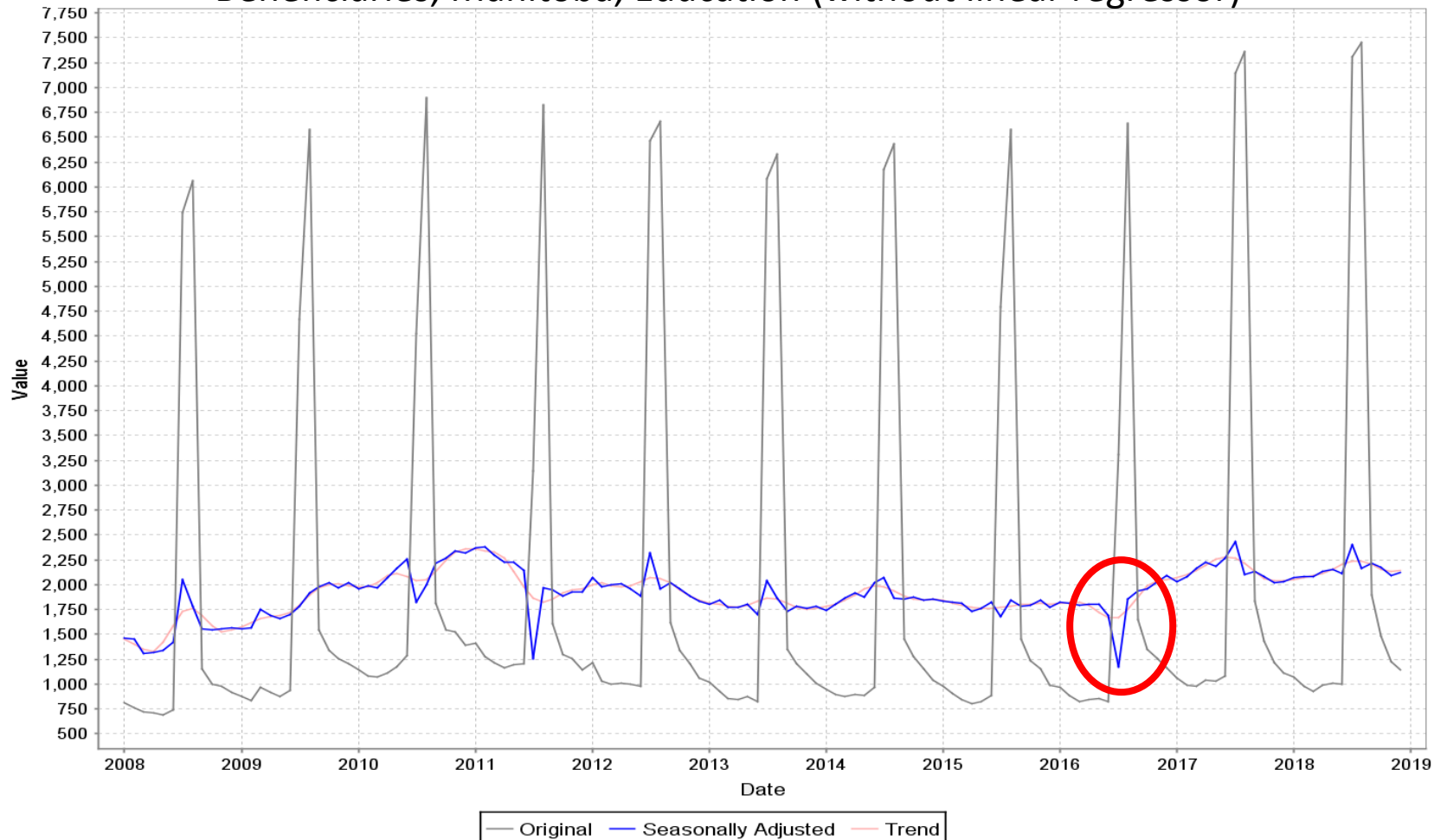


## Solution 2: Use Detailed Data

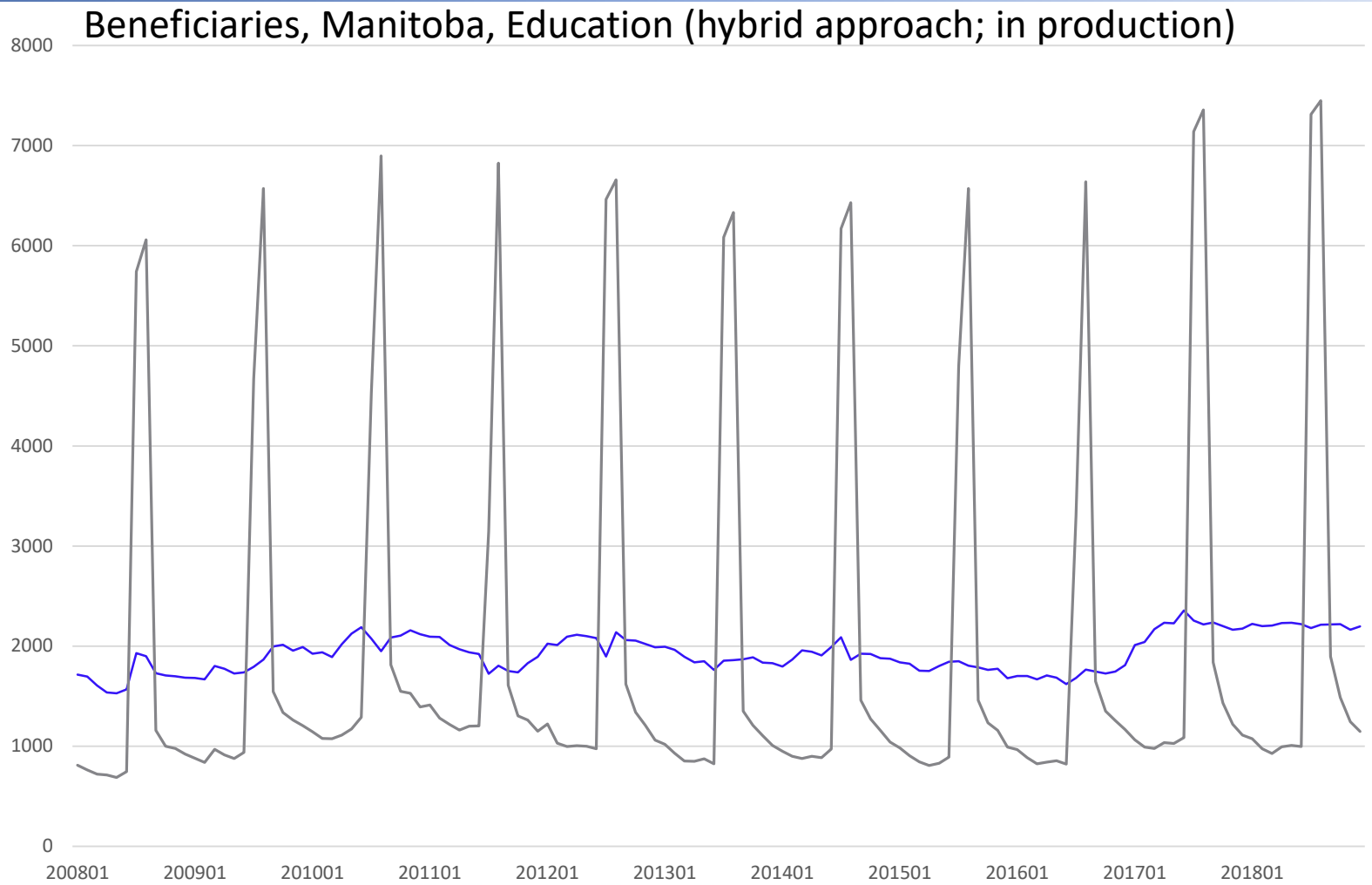
- Pretend beneficiaries prior to 2017 had one-week waiting period (we know the date when people applied for EI)
- Since reference week adjustment works well for up to end of 2016, we would do seasonal adjustment in 2 parts:
  - Prior to 2017: use the linear regARIMA model
  - Use the information from the detailed data where we pretend we have a 1-week period up to end of 2016, and use the actual data in 2017 onward.
- Results are better and results in smoother graphs with no spikes.

# Solution 2: Use Detailed Data

Beneficiaries, Manitoba, Education (without linear regressor)



# Solution 2: Use Detailed Data



# Conclusion

- Discontinuity and spike in our data gave us issues in seasonal adjustment.
- 2 solutions considered: modelling and alternative data source.
  - The hybrid model we chose in the end removed spikes and worked well.
- Maintain the linear models for now
  - There may be potential for considering the other models (perhaps quadratic) and may leave the door open to other models when we get more data.





Thank You!

Questions?

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